

11/8/05

10/525970

DT06 Rec'd PCT/PTO 2 8 FEB 2005

### Satellite-based navigation method

The invention relates to a satellite-based navigation method for the determination of the position of a receiver by ascertaining the signal propagation time between preferably at least two satellites and the receiver.

As a rule, in satellite-based navigation the signal propagation time between several satellites and the receiver is determined and therefrom the position of the receiver is calculated. For each satellite  $i$  from the relation  $c \cdot (T_{\text{receiver}} - T_{\text{transmitter}})$  the pseudo-distance is determined

$$\rho_i = \sqrt{(\bar{x}_i - \bar{x})^2} + c \cdot \Delta t + \varepsilon$$

where  $x_i$  is the position of satellite  $i$ ,  $\bar{x}$  the position of the receiver,  $c$  the speed of light,  $\Delta t$  the time error of the receiver clock and  $\varepsilon$  other errors (such as orbit and clock errors of the satellite, propagation time errors due to atmospheric conditions or other errors of measurement of the receiver).

In general, for reasons of cost in the receiver highly precise time references are omitted, such that the dominant error in position determination is the time error  $\Delta t$  in the receiver clock. This time error is included in the calculation of position.

Therefore, for the position determination at least four satellite signals are required in order to determine the three spatial coordinates and the time error and to determine therefrom  $T_{\text{receiver}}$ .

Through differential satellite navigation methods errors in the satellite segment and propagation time errors due to atmospheric conditions can be detected and largely compensated. If redundant information is available, i.e. if for a three-dimensional position determination more than four satellites and for a one-dimensional, track-guided position determination more than two satellites are received, through RAIM

algorithms (Receiver Autonomous Integrity Monitoring) in the receiver an error self-detection can be carried out, which uncovers propagation time errors of the received satellites. If, however, the signal propagation times to several satellites are falsified, these errors cannot always be detected with certainty such that, in spite of the RAIM algorithm, unrecognized false position determinations result.

The aim of the present invention lies in improving the integrity of the position solution, i.e. to decrease the probability of calculation of a false position specification.

This aim is attained through a satellite-based navigation method of the above type essentially thereby that the receiving time of satellite signals at the receiver (1, 5) is determined by means of a precise time reference in the receiver (1, 5) as well as also from the satellite signals and these are compared with one another. Equipping the receiver with a precision clock, for example a rubidium clock, makes available a highly precise time reference in order to determine the receiving time highly precisely. By comparison of receiving times ascertained in different ways it is therefore possible to recognize whether interferences are present during the reception of the signals. With this method, thus through the reception of at least two or three satellite signals in track-guided or surface-bound systems indirect signals can also be recognized, which, due to the shadowing off of the direct signal from satellite to receiver, are only received via a reflected signal. In this case the pseudo-distance

$$\rho_i = \sqrt{(\bar{x}_i - \bar{x}_R)^2 + (\bar{y}_i - \bar{y}_R)^2} + \sqrt{(\bar{x}_R - \bar{x})^2 + (\bar{y}_R - \bar{y})^2} + c \cdot \Delta t + \varepsilon$$

is correspondingly longer,  $\bar{x}_R$  being the position of the reflector. If such shadowing off is not recognized and the signal is utilized for position calculation, an erroneous position determination results. Depending on the position of the satellites relative to the receiver, in contrast, with the present invention the time offset due to the reflection can be recognized. In addition, the time error  $\Delta t$  dominating in the pseudo-

distance  $\rho_i$  of the receiver clock is not applicable, such that the pseudo-distance is determined more precisely and the reception of at least four satellite signals for the three spatial coordinates and the time error are no longer required. In this case a three-dimensional position determination can already be realized with three satellite signals. If the receiver can only move along a known track, for example in the position determination for trains bound to the rail network, according to the conventional method, it is already sufficient to determine only two unknowns, namely the track-kilometer and the time offset. In this case two satellites suffice for the position determination. If, in contrast, according to the invention the receiver is equipped with a highly precise clock, which, as a rule, is omitted for reasons of cost, the time offset no longer needs to be determined, such that in principle even only one satellite for each determined coordinate is sufficient.

The present invention also relates to a satellite-based navigation method for determining the position of a receiver by ascertaining the signal propagation time between satellites and the receiver, in which at least two position solutions are determined from the reception time of the satellite signals at the receiver ascertained by means of a precise time reference of the receiver, and the satellite signals from at least two different satellites, and compared with one another. In particular with track-guided systems for at least two satellites, from one satellite signal for each and the time reference of the receiver, a position solution of the receiver can be determined. Similarly to the previously described method, subsequently, depending on the position of the satellites, such signals can be recognized which have only been received over indirect paths. A combination of the two previously described methods can furthermore be of advantage.

In order to obtain no error in the position determination through reflected signals, according to the invention satellite signals are only drawn on for the position determination if the difference between the reception time, determined from the satellite signals and from the time difference and/or the difference between two

position solutions determined from satellite signals does not exceed a tolerance value which can be specified in each instance. The tolerance value results substantially from the maximum pseudo-distance errors of the corresponding satellites. If this tolerance value is exceeded, at least one of the signals has been received on an indirect path.

If reflected satellite signals are also drawn on for position determination, the invention provides that a position interval is determined if the difference between the reception time determined from the satellite signals and from the time reference and/or the difference between two position solutions determined from satellite signals exceeds a tolerance value which in each instance can be specified. Therewith an interval can be determined, which includes the actual position such that the user recognizes precisely the uncertainty in the position determination.

In a track-guided receiver the method can be utilized with special advantage if satellite signals from two satellites are evaluated whose positions at the reception of the satellite signals are determined by a first angle  $\vartheta_1$  between the direction of motion of the receiver and the connection direction from the receiver to a first satellite in an angular range of  $0^\circ < \vartheta_1 < 90^\circ$  and by a second angle  $\vartheta_2$  between the direction of motion of the receiver and the connection direction from the receiver to a second satellite in an angular range of  $90^\circ < \vartheta_2 < 180^\circ$ . Consequently, in this case at least one satellite in the forward and rearward direction each is received. In this case an indirect satellite signal, which has been reflected before the reception by the receiver from an arbitrary reflector, can be recognized with certainty.

For this purpose preferably for the ascertaining of the reception time from the satellite signals of the first and of the second satellite the position and the time offset error of a pseudo-range measurement are determined. By comparison of the ascertained reception time and the actual reception time known from the precise time

reference, indirect signals are recognized with certainty if a specified tolerance value is being exceeded.

In a surface-bound receiver, i.e. a receiver moving on a determinate surface, in one embodiment of the method according to the invention satellite signals from three satellites are evaluated, whose position is determined by a first angle  $\varphi_1$  for the first satellite, a second angle  $\varphi_2$  for the second satellite and a third angle  $\varphi_3$  for the third satellite, the angles being the azimuth angle of the connection directions projected onto the base plane of a system of coordinates, from the receiver to the particular satellites and have the following relations to one another,

$0^\circ < \varphi_2 - \varphi_1 < 180^\circ$  and  $0^\circ < \varphi_3 - \varphi_2 < 180^\circ$  and  $360^\circ > \varphi_3 - \varphi_1 > 180^\circ$ . In this case indirect signals can be established with certainty.

The base surface of the system of coordinates is preferably in a plane which at the position of the receiver is tangential to a surface on which the receiver moves. In such a system of coordinates the  $0^\circ$  direction can be for example in the direction of motion of the body. This system of coordinates can be uniquely determined and is therefore especially suitable for the designation of the satellite positions. However, corresponding angular positions can also be defined in differently selected systems of coordinates.

In the case of this method variant of the present invention the reception time for the establishment of indirect signals can also be ascertained especially reliably from the satellite signals of the first, second and third satellites by determining the position and time offset errors of a pseudo-range measurement.

In order to increase further the integrity of the position solutions, a satellite-based integrity system, such as for example EGNOS or WAAS can be utilized. Further,

accuracy and integrity of the position solutions can be further improved through differential operation or by means of DGPS.

With reference to the drawing preferred method variants of the method according to the invention will be described in the following. Further advantages and characteristics of the present invention are evident therein, also independently of the summary of the characteristics in the claims or their references back.

In the drawing depict:

Fig. 1            the condition in the application of the method according to the invention for a track-guided receiver and

Fig. 2            the condition in the application of the method according to the invention for a surface-bound receiver.

Fig. 1 shows a receiver 1 which moves in the direction indicated by an arrow along a track 2. The receiver 1 can be located for example in a train and receive signals from two satellites 3, 4, which, for the position determination of the receiver 1, are located on the track 2 in space. Both satellites 3, 4 are sending satellite signals which are being received by the receiver 1. The receiver 1 comprises additionally a (not shown) highly precise time reference, which precisely defines the reception time of the satellite signals from satellites 3, 4. This time reference can be, for example, a highly precise rubidium clock, which determines the time with an accuracy of approximately  $10^{-11}$  to  $10^{-9}$  sec. For longer time intervals the accuracy may be degraded such that only larger errors of the pseudo-distance measurement are detected. The measuring principle, however, remains also in this case applicable. In the case of this track-guided receiver 1 the position errors  $\delta x$  along track 2, the error  $\Delta t$  in the time offset and the pseudo-range error  $\delta R$  are related as follows

$$\delta R = c \cdot \Delta t + \cos(\theta_i) \cdot \delta x,$$

where  $\vartheta_i$  is the angle between track 2 and the direction from the receiver 1 to the satellites 3, 4 and  $c$  the speed of light.

If, as in the depicted case, satellite 3 is in the forward direction with respect to the position of receiver 1 and satellite 4 in the rearward direction, it is possible to establish the presence of an indirect satellite signal, which before the reception in receiver 1 was scattered at a reflector. This applies whenever the angle  $\vartheta_1$  is between  $0^\circ$  and  $90^\circ$  in the forward direction and angle  $\vartheta_2$  between  $90^\circ$  and  $180^\circ$  in the rearward direction.

From the satellite signals the position along track 2 is determined through two pseudo-range measurements, where as position error

$$\delta x = \frac{\delta R_1 - \delta R_2}{\cos \theta_1 - \cos \theta_2}$$

and as time offset error

$$c \cdot \Delta t = \frac{\cos \theta_1 \cdot \delta R_2 - \cos \theta_2 \cdot \delta R_1}{\cos \theta_1 - \cos \theta_2}$$

is obtained. From the time offset error subsequently the reception time of signal  $T_{\text{receiver}}$  is calculated. This is compared with the reference time  $T_{\text{ref}}$  ascertained by the highly precise clock. If

$$T_{\text{receiver}} - T_{\text{ref}} > \left| \frac{\cos \theta_1 \cdot \varepsilon_{1,\text{max}}}{\cos \theta_1 - \cos \theta_2} \right| + \left| \frac{\cos \theta_2 \cdot \varepsilon_{2,\text{max}}}{\cos \theta_1 - \cos \theta_2} \right| + \varepsilon_{R,\text{max}}$$

applies, at least one of the two satellite signals has been received on an indirect path, where  $\varepsilon_{1,\max}$  and  $\varepsilon_{2,\max}$  represent the maximum values of the pseudo-distance error and  $\varepsilon_{R,\max}$  the maximum error of the time reference. These are caused by satellite errors, atmospheric effects and receiver errors (except the clock time) and are a function of the receiver 1 utilized and, with differential navigation methods, additionally from the distance from the reference station(s). A position calculated from an indirect satellite signal would, as a rule, be false.

Alternatively or supplementally to the previously described methods, for each satellite 3, 4 the position along path [sic: track] 2 can be calculated from the pseudo-distance and the precise time reference of receiver 1. Indirect satellite signals from satellite 3 in the forward direction lead to a position error in the rearward direction. Conversely, indirect signals from satellite 4 in the rearward direction cause a position error in the forward direction.

If for satellite 3 in the forward direction and satellite 4 in the rearward direction the difference of the positions

$$\left| \frac{\varepsilon_{1,\max} + \varepsilon_{R,\max}}{\cos \theta_1} \right| + \left| \frac{\varepsilon_{2,\max} + \varepsilon_{R,\max}}{\cos \theta_2} \right|$$

exceeds [tolerance], at least one indirect signal is present, which can lead to a false position determination.

If indirect satellite signals in a track-guided receiver 1 are to be established in every case, in the satellite signals of satellites 3, 4 to be drawn on for the navigation method, it must be ensured that the angle  $\theta_1$  with respect to the satellite 3 is in the range between  $0^\circ$  and  $90^\circ$  and angle  $\theta_2$  with respect to satellite 4 in the range between



90° and 180°. Signals from satellites which are both positioned in the forward or rearward direction are in this case not drawn on together for the navigation method.

The method can alternatively be implemented such that the position determination is carried out with two arbitrary satellite signals and - if one satellite 3 is in the forward and one satellite 4 in the rearward direction - additionally the checking for indirect signals is carried out.

In the case of redundant satellite signals satellites 3, 4 can also be determined through suitable combination of two satellites 3, 4 of which one satellite is in the forward and one in the rearward direction, which had only been received via an indirect path. These can subsequently be neglected in the determination of the position solution.

If it is not possible to identify satellites 3, 4 unambiguously, which had been received directly, an interval can nevertheless be determined which includes the actual position. This track interval can be determined as described in the following.

For a satellite 3 in forward direction and a satellite 4 in rearward direction, from the pseudo-distance and the time reference two positions P1 and P2 along the track are calculated, where  $P_1 > P_2$ . In this case the interval

$$\left[ P_2 - \left| \frac{\varepsilon_{2,\max} + \varepsilon_{R,\max}}{\cos \theta_2} \right|, P_1 + \left| \frac{\varepsilon_{1,\max} + \varepsilon_{R,\max}}{\cos \theta_1} \right| \right]$$

includes the actual position.

A corresponding method is illustrated in Fig. 2 for a receiver 5, which moves on a surface 6 in the direction indicated by an arrow. This receiver 5 receives satellite signals from satellites 7, 8 and 9, and the receiver 5 can be determined very precisely the

reception time of the satellite signals through a (not shown) highly precise time reference. The accuracy of the time reference is typically again in the same range.

If [sic: omit] During the reception of the satellite signals the position of satellites 7, 8, 9 are determined through a first angle  $\varphi_1$  for the first satellite 7, a second angle  $\varphi_2$  for the second satellite 8 and a third angle  $\varphi_3$  for the third satellite 9, where the angles  $\varphi_1$ ,  $\varphi_2$ ,  $\varphi_3$  are the azimuth angles of the connection directions, projected onto the base plane 10 of a system of coordinates, from the receiver 5 to the particular satellites 7, 8, 9 and are related  $0^\circ < \varphi_2 - \varphi_1 < 180^\circ$ ,  $0^\circ < \varphi_3 - \varphi_2 < 180^\circ$  and  $360^\circ > \varphi_3 - \varphi_1 > 180^\circ$  one to another. The base surface [sic] 10 of the system of coordinates is in a plane which, at the position of receiver 5, is tangential to the movement surface 6 of the receiver 5. The satellites 7, 8, 9 are sorted such that  $0^\circ \leq \varphi_1 < \varphi_2 < \varphi_3 < 360^\circ$  applies.

If, in this constellation, the position of receiver 5 on surface 6 is determined by three pseudo-range measurements then, as time offset error is obtained

$$c \cdot \Delta t = \frac{|x_1^p| \cdot |x_2^p| \cdot \sin(\varphi_2 - \varphi_1) \cdot \delta R_3 + |x_2^p| \cdot |x_3^p| \cdot \sin(\varphi_3 - \varphi_2) \cdot \delta R_1 + |x_3^p| \cdot |x_1^p| \cdot \sin(\varphi_1 - \varphi_3) \cdot \delta R_2}{|x_1^p| \cdot |x_2^p| \cdot \sin(\varphi_2 - \varphi_1) + |x_2^p| \cdot |x_3^p| \cdot \sin(\varphi_3 - \varphi_2) + |x_3^p| \cdot |x_1^p| \cdot \sin(\varphi_1 - \varphi_3)},$$

where  $\hat{x}_i$  is a unit vector in the direction from receiver 5 to one of the satellites 7, 8, 9 ( $i=1, 2, 3$ ),  $x_i^p$  the projection of  $\hat{x}_i$  onto the base plane 10 and  $\varphi_i$  the azimuth angle of  $x_i^p$  in the base plane 10. The three-dimensional spherical system of coordinates is located such that the x direction extends in the direction of motion of receiver 5 and the z direction normal with respect to the base surface 10. From the time offset error subsequently the reception time  $T_{\text{receiver}}$  is determined and compared with the reference time  $T_{\text{ref}}$ . In the case

$$\begin{aligned} & T_{\text{receiver}} - T_{\text{ref}} \\ & > \frac{|x_1^p| \cdot |x_2^p| \cdot \sin(\varphi_2 - \varphi_1) \cdot \varepsilon_{3,\max} + |x_2^p| \cdot |x_3^p| \cdot \sin(\varphi_3 - \varphi_2) \cdot \varepsilon_{1,\max} + |x_3^p| \cdot |x_1^p| \cdot \sin(\varphi_1 - \varphi_3) \cdot \varepsilon_{2,\max}}{|x_1^p| \cdot |x_2^p| \cdot \sin(\varphi_2 - \varphi_1) + |x_2^p| \cdot |x_3^p| \cdot \sin(\varphi_3 - \varphi_2) + |x_3^p| \cdot |x_1^p| \cdot \sin(\varphi_1 - \varphi_3)} + \varepsilon_{R,\max} \end{aligned}$$

applies, at least one of the three satellite signals has been received on an indirect path.

In the presence of redundant satellite signals, through suitable combination of, in each instance, three satellites 7, 8 and 9, which fulfill the aforementioned position conditions, those satellites can be determined which have only been received via indirect paths. These satellites can subsequently be neglected in the determination of the position solution.

In the case of a suitable position of satellites 3, 4 or 7, 8, 9, respectively, with the navigation method of the present invention such satellite signals can be sought out, which had not been received directly from one of satellites 3, 4, 7, 8, 9 at a receiver 1, 5, but had only reached the receivers 1, 5 on an indirect path via a reflector. Thereby the integrity of the navigation method is increased. These errors cannot be detected through differential operation or satellite-based integrity systems.

Therefore the method according to the invention can in general be especially well employed for the position calculation in land and sea navigation. A special employment lies in rail traffic in the determination of confidence intervals, as well as in all employments for which special reliability is required, such as for example docking methods of ships, airplanes or like craft.

### List of Reference Numbers

1	Receiver
2	Track
3	Satellite
4	Satellite
5	Receiver
6	Surface
7	Satellite
8	Satellite
9	Satellite
10	Base plane